Family-based model checking of FMULTILTL properties

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ABSTRACT

We introduce a new logic for expressing multi-properties of system families (Software Product Lines - SPLs). While the standard LTL logic refers only to a single trace at a time, FMULTILTL logic proposed here refers to multiple traces originating from different sets of variants of the SPL. This is achieved by allowing so-called *featured quantification* over traces, \forall^{ψ} and \exists^{ψ} , where the feature expression ψ describes a set of variants (sub-family) the quantified trace comes from. A specialized family-based model checking algorithm for verifying some fragments of FMULTILTL is given. A prototype family-based model checker, called DÆDALUX, has been implemented. We illustrate the practicality of this approach on several interesting SPL models.

CCS CONCEPTS

• Software and its engineering \rightarrow Software notations and tools; Software creation and management; • Theory of computation \rightarrow Semantics and reasoning.

KEYWORDS

Software Product Lines, Model Checking, LTL, Temporal Multi-Properties,

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1 INTRODUCTION

Software Product Line Engineering (SPLE) [14, 44] represents an efficient method for building families of similar systems. Implementations of such *system families* use *features* (statically configured options) to organize the variable functionality. Family members,

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called *variants*, are specified in terms of features selected for that particular variant. The reuse of code common to multiple variants is thus maximized. In the past decade, the SPL method has grown in popularity, especially in the domains of embedded systems, system-level software, communication protocols, etc [14].

In many application domains, such as automotive and avionics, quality assurance is of predominant importance. This requires a solid evidence that system families indeed satisfy their specifications. Researchers have addressed this problem by designing compact representations for modelling the behaviour of all variants of a system family in a single compact structure, and by designing aggregate family-based model checking algorithms to efficiently verify such compact representations. In particular, the family-based model checking algorithms allow simultaneous verification of all variants of a system family in a single run by exploiting the commonalities between the variants. Those algorithms are capable of identifying all variants that satisfy a property, as well as all variants that do not satisfy the property together with the corresponding counter-examples. Specialized family-based model checking algorithms have been developed for various modelling formalisms: reactive [10, 11, 17, 26, 48], real-time [15, 33], probabilistic [6] systems, as well as for verification of properties in various temporal logics: linear-time temporal logic LTL [10, 11, 26], computation tree logic CTL* [17, 22, 32], µ-calculus [47].

The LTL is a logic for expressing trace properties. However, some behaviors cannot be expressed by referring to each trace individually. For example, secure information flow and non-interference [3, 49] are maintained in a system if for every two traces, if their low-security inputs are identical then so are their low security outputs, regardless of their high-security variables. They cannot be characterized via single traces. In fact, they cannot be expressed neither in CTL^{*} nor in μ -calculus. In [7, 35, 37], properties describing the behaviour of a combination of traces are introduced. They are known as hyper-properties (HYPERLTL) [7, 35] when different traces refer to the same system, and *multi-properties* (MULTILTL) [37] when different traces refer to different components of a system. That is, MULTILTL enable us to relate traces from one component (sub-system) to traces of another component of a compound system. We now extend the notion of MULTILTL in the context of system families and SPLs, thus obtaining the so-called *featured* MULTILTL, denoted by FMULTILTL.

In this paper, we introduce a new logic FMULTILTL for specifying multi-properties of system families and we study algorithms for their automatic verification. FMULTILTL generalizes LTL by

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explicitly relating traces from different variants of a system family. While LTL implicitly quantifies over only a single execution trace of a system, FMULTILTL allows explicit quantification over multiple execution traces of a system family simultaneously, as well as propositions that specify relationships among those traces. In particular, FMULTILTL allows featured quantification, \forall^{ψ} and \exists^{ψ} , referring to the sub-family (a set of variants) described by the feature expression ψ . This way, traces from the sub-family described by ψ can be referred to in the atomic propositions. Since a system family consists of a set of similar systems, FMULTILTL properties will enable us to relate traces from one subset of systems to another subset. For example, the *diversity* property [45] asks all systems from a family to represent a different implementation of the same high-level system. That is, all systems implement the same functionality but differ in their implementation details. Diversity has been used as a security property to resist attacks that exploit memory layout or instruction sequence specifics. Given a high-level system described with the base feature, and two low-level implementations described with features f1 and f2 respectively, the diversity property can be expressed as:

$$\begin{array}{l} \varphi_1 = \forall_{\pi_0}^{\text{base}} \exists_{\pi_1}^{-1} \exists_{\pi_2}^{-2}.\Box \left(\text{in}_{\pi_0} = \text{in}_{\pi_1} = \text{in}_{\pi_2} \implies \text{out}_{\pi_0} = \text{out}_{\pi_1} = \text{out}_{\pi_2} \right) \\ \varphi_2 = \forall_{\pi_1}^{-1} \exists_{\pi_0}^{\text{base}}.\Box \left(\text{in}_{\pi_1} = \text{in}_{\pi_0} \implies \text{out}_{\pi_1} = \text{out}_{\pi_0} \right) \\ \varphi_3 = \forall_{\pi_0}^{-2} \exists_{\pi_0}^{\text{base}}.\Box \left(\text{in}_{\pi_2} = \text{in}_{\pi_0} \implies \text{out}_{\pi_2} = \text{out}_{\pi_0} \right) \end{array}$$

where $in_{\pi_0} = in_{\pi_1} = in_{\pi_2}$ and $out_{\pi_0} = out_{\pi_1} = out_{\pi_2}$ express that the three traces π_0 , π_1 , π_2 agree on the input and output variables in and out, respectively. Note that the traces π_0 , π_1 , and π_2 come from the systems that contain features base, f1 and f2, respectively. Our FMULTILTL logic enables to directly and naturally express properties like the one above.

We present family-based model checking algorithms applicable to restricted type of FMULTILTL properties, called alternation-free FMULTILTL, in which the series of quantifiers at the beginning of a formula involve zero alternation. Finally, we have implemented a prototype tool within DAEDALUX, a new-generation SPL model checking platform, and we practically evaluated the algorithms for verifying the alternation-free fragment of FMULTILTL. This is a useful fragment which allows specifying many interesting properties of system families.

To summarize, our contributions are as follows:

- We define a new logic FMULTILTL for expressing properties that specify relations over multiple traces from various sets of variants of a system family;
- (2) We propose a specialized family-based model checking algorithm for automatic verification of alternation-free fragment of FMULTILTL;
- (3) We describe a prototype implementation of our familybased model checking algorithm and use it to verify some interesting alternation-free FMULTILTL properties of system families.

2 BACKGROUND: SYSTEM FAMILIES

In this section, we summarize the existing background for our work. We present modelling formalisms used to compactly represent system families, and define their semantics. Let $\mathcal{F} = \{A_1, \ldots, A_n\}$ be a finite set of Boolean variables representing the features available in a system family. A specific subset of features, $k \subseteq \mathcal{F}$, known as *configuration*, specifies a *variant* of a system family. We assume that only a subset $\mathcal{K} \subseteq 2^{\mathcal{F}}$ of configurations are *valid*. An alternative representation of configurations is based upon propositional formulae. Each configuration $k \in \mathcal{K}$ can be represented by a formula: $v(A_1) \land \ldots \land v(A_n)$, where $v(A_i) = A_i$ if $A_i \in k$, and $v(A_i) = \neg A_i$ if $A_i \notin k$ for $1 \le i \le n$. We will use both representations interchangeably.

We use *transition systems* (TS) to describe behaviors of single systems. A *transition system* is a tuple $\mathcal{T} = (S, Act, I, trans, AP, L)$, where S is a set of states; $I \subseteq S$ is a set of initial states; $trans \subseteq S \times Act \times S$ is a transition relation which is *total*, so that for each state there is an outgoing transition; AP is a set of atomic propositions; and $L : S \to 2^{AP}$ is a labelling function specifying which atomic propositions hold in a state. We write $s_1 \xrightarrow{\lambda} s_2$ when $(s_1, \lambda, s_2) \in trans$. A *path* of a TS \mathcal{T} is an *infinite* sequence $\rho = s_0 s_1 s_2 \dots$ with $s_0 \in I$ such that $s_i \xrightarrow{\lambda_{i+1}} s_{i+1}$ for all $i \ge 0$ ($\lambda_{i+1} \in Act$). A *trace* corresponding to the path $\rho = s_0 s_1 s_2 \dots$ is the sequence of sets of propositions trace(ρ) = $L(s_0)L(s_1)L(s_2) \dots$. The *semantics* of the TS \mathcal{T} , denoted as $[[\mathcal{T}]]_{TS}$, is the set of its traces.

A *featured transition system* (FTS) represents a compact model, which describes the behavior of a whole family of systems in a single monolithic description. Their transitions are guarded by a *presence condition* that identifies the variants they belong to. The presence conditions ψ are drawn from the set of feature expressions, *FeatExp*(\mathcal{F}), which are propositional logic formulae over \mathcal{F} :

$$\psi ::= true \mid A \in \mathcal{F} \mid \neg \psi \mid \psi_1 \land \psi_2$$

We write $[[\psi]]$ for the set of configurations that satisfy ψ , i.e. $k \in [[\psi]]$ iff $k \models \psi$.

A featured transition system (FTS) is defined to be a tuple $\mathbb{F}=$ $(S, Act, I, trans, AP, L, \mathcal{F}, \mathcal{K}, \gamma)$, where (S, Act, I, trans, AP, L) form a TS; \mathcal{F} is a set of available features; \mathcal{K} is a set of valid configurations; and γ : trans \rightarrow FeatExp(\mathcal{F}) is a total function decorating transitions with presence conditions (feature expressions). The projection of an FTS \mathbb{F} to a configuration $k \in \mathcal{K}$, denoted as $Pr_k(\mathbb{F})$, is the TS (S, Act, I, trans', AP, L), where trans' = $\{t \in trans \mid k \models \gamma(t)\}$. We lift the definition of *projection* to sets of configurations $\mathcal{K}' \subseteq \mathcal{K}$, denoted as $Pr_{\mathcal{K}'}(\mathbb{F})$, by keeping the transitions admitted by at least one of the configurations in \mathcal{K}' . That is, $Pr_{\mathcal{K}'}(\mathbb{F})$, is the FTS $(S, Act, I, trans', AP, L, \mathcal{F}, \mathcal{K}', \gamma')$, where $trans' = \{t \in trans \mid \exists k \in trans \mid d \in tras \mid d \in trans \mid d \in trans \mid d \in trans \mid d$ $\mathcal{K}'.k \models \gamma(t)$ and $\gamma' = \gamma|_{trans'}$ is the restriction of γ to *trans'*. The semantics of an FTS \mathbb{F} , denoted as $[[\mathbb{F}]]_{FTS}$, is the union of traces of transition systems representing the projections $Pr_k(\mathbb{F})$ on all valid variants $k \in \mathcal{K}$. That is, $[[\mathbb{F}]]_{FTS} = \bigcup_{k \in \mathcal{K}} [[Pr_k(\mathbb{F})]]_{TS}$. Moreover, the semantics of the projection FTS $Pr_{\mathcal{K}'}(\mathbb{F})$ is $[[Pr_{\mathcal{K}'}(\mathbb{F})]]_{FTS} =$ $\cup_{k\in\mathcal{K}'} [[\pi_k(\mathbb{F})]]_{TS}.$

Example 2.1. The FTS VENDMACHINE in Fig. 1 has features $\mathcal{F} = \{\text{base, } v, t, s, c, f\}$. The feature base is used only for implementing the high-level system and is not present in other configurations. The set of all other valid configurations is obtained by combining the above features (except base). The feature v is for purchasing a drink from the Vending machine; s is for serving Soda; t is for serving Tea; c is for Canceling a purchase after a coin is entered; and f is for offering Free drinks. Each transition is labeled by a



Figure 1: The FTS VENDMACHINE.



Figure 2: TSs $Pr_{\{v,s\}}$ (VENDMACHINE) (left) and $Pr_{\{base\}}$ (VENDMACHINE) (right).



Figure 3: The FTS $Pr_{[[v \land s]]}$ (VENDMACHINE).

feature expression specifying in which variants the transition is included. For instance, the transition (3) $\xrightarrow{soda/s}$ (5) is included in variants where feature *s* is enabled. The feature *v* is mandatory, and at least one of *s* or *t* is enabled in any valid configuration. The set of valid configurations is thus:

$$\mathcal{K}^{VM} = \{ \{ base \}, \{v, s\}, \{v, t\}, \{v, s, t\}, \{v, s, c\}, \{v, t, c\}, \{v, s, t, c\}, \{v, s, t, c\}, \{v, s, t, f\}, \{v, s, t, f\}, \{v, s, c, f\}, \{v, t, c, f\}, \{v, s, t, c, f\} \}.$$

Figure 2 shows two variants of VENDMACHINE: a version that only serves soda, and a high-level implementation. The former variant is described by the configuration: $\{v, s\}$, equivalently as a formula: $\neg base \land v \land s \land \neg t \land \neg c \land \neg f$. The model presented in the figure is obtained by the projection $Pr_{\{v,s\}}$ (VENDMACHINE). It accepts payment, returns change, serves a soda, opens the access compartment, so that the user can take the soda, and close it again so that a next user can be served. The latter variant is described by the configuration: $\{base\}$, equivalently as a formula: $base \land \neg v \land \neg s \land \neg t \land \neg c \land \neg f$. Its model is obtained by $Pr_{\{base\}}$ (VENDMACHINE).

On the other hand, note that $[[v \land s]] = \{k \in \mathcal{K}^{VM} \mid k \models v \land s\} = \{\{v, s\}, \{v, s, t\}, \{v, s, c\}, \{v, s, t, c\}, \{v, s, t, f\}, \{v, s, c, f\}, \{v, s, t, c, f\}\}$ represents a sub-family of VENDMACHINE. The FTS $Pr_{[[v \land s]]}$ (VENDMACHINE) is shown in Fig. 3. Note that transition

(1) $\xrightarrow{select/base}$ (3) is not present in this FTS, since it is not present in any variant from [[$v \land s$]]. To simplify notation, all literals v and s in feature expressions in $Pr_{[[v \land s]]}$ (VENDMACHINE) are replaced with *true* (see Fig. 3), since they evaluate to *true* in any variant from [[$v \land s$]]. □

3 FMULTILTL PROPERTIES

We now present *featured* MULTILTL, denoted FMULTILTL, a logic for describing multi-properties of system families described by FTSs. FMULTILTL extends LTL with explicit quantification over traces. It is defined inductively as follows:

$$\begin{split} \varphi &::= \exists^{\psi} \pi. \varphi \mid \forall^{\psi} \pi. \varphi \mid \phi \\ \varphi &::= a_{\pi} \mid \neg \phi \mid \phi_1 \land \phi_2 \mid \bigcirc \phi \mid \phi_1 \cup \phi_2 \end{split}$$

where π is a trace variable, $\psi \in FeatExp(\mathcal{F})$, and $a \in AP$. Intuitively, $\exists^{\psi} \pi. \varphi$ means that there exists a trace in the sub-family $Pr_{[[\psi]]}(\mathbb{F})$ that satisfies φ , and $\forall^{\psi} \pi. \varphi$ means that φ holds for every trace in $Pr_{[[\psi]]}(\mathbb{F})$. Atomic propositions $a \in AP$ are annotated with trace variables π , denoted a_{π} , to disambiguate to which trace the proposition refers to. A formula φ is *closed* if all trace variables π are in the scope of a quantifier. Boolean connectives disjunction (\vee) , implication (\Longrightarrow), and equivalence (\equiv) are defined as syntactic sugar. The other temporal operators are also defined by means of ,

syntactic sugar, for instance: $\Diamond \phi = true \cup \phi$ (ϕ holds eventually) and $\Box \phi = \neg \Diamond \neg \phi$ (ϕ always holds).

Formally, the semantics of FMULTILTL is defined as follows. Let $Tr \subseteq (2^{AP})^{\omega}$ be a set of all traces and let $t \in Tr$ be a trace. We use t[i] to denote the *i*-th element of *t*. We write t[0, i] to denote the prefix of *t* up to and including *i*-th element, and $t[i, \infty]$ to denote the infinite suffix of *t* beginning with *i*-th element. The satisfaction $\mathbb{F} \models \varphi$ is given in terms of *trace assignment* $\Pi : V \to Tr$, which represents a mapping from trace variables *V* to traces Tr. Let $\Pi[\pi \mapsto t]$ be the function obtained from Π , by mapping a trace variable $\pi \in V$ to a trace $t \in Tr$. Let Π^i be the function defined by $\Pi^i(\pi) = (\Pi(\pi))[i, \infty]$. Satisfaction of a formula φ for an FTS \mathbb{F} and a trace assignment Π is defined as:

$$\begin{split} \Pi &\models_{\mathbb{F}} \exists^{\psi} \pi.\varphi \text{ iff } \exists t \in [[Pr_{[[\psi]]}(\mathbb{F})]]_{\text{FTS}}.\Pi[\pi \mapsto t] \models_{\mathbb{F}} \varphi \\ \Pi &\models_{\mathbb{F}} \forall^{\psi} \pi.\varphi \text{ iff } \forall t \in [[Pr_{[[\psi]]}(\mathbb{F})]]_{\text{FTS}}.\Pi[\pi \mapsto t] \models_{\mathbb{F}} \varphi \\ \Pi &\models_{\mathbb{F}} a_{\pi} \text{ iff } a \in \Pi(\pi)[0] \\ \Pi &\models_{\mathbb{F}} \neg \phi \text{ iff } \Pi \not\models_{\mathbb{F}} \phi \\ \Pi &\models_{\mathbb{F}} \phi_{1} \land \phi_{2} \text{ iff } \Pi \models_{\mathbb{F}} \phi_{1} \text{ and } \Pi \models_{\mathbb{F}} \phi_{2} \\ \Pi &\models_{\mathbb{F}} \bigcirc \phi \text{ iff } \Pi^{1} \models_{\mathbb{F}} \phi \\ \Pi &\models_{\mathbb{F}} (\phi_{1} \cup \phi_{2}) \text{ iff } \exists i \geq 0. (\Pi^{i} \models_{\mathbb{F}} \phi_{2} \land \forall j.0 \leq j < i. \Pi^{j} \models_{\mathbb{F}} \phi_{1} \end{split}$$

A FTS \mathbb{F} satisfies a closed formula φ , written $\mathbb{F} \models \varphi$, if $\Pi_{\emptyset} \models_{\mathbb{F}} \varphi$ where Π_{\emptyset} is the empty trace assignment with empty domain. That is, when φ is closed, i.e. all trace variables are in the scope of a quantifier, then the satisfaction of φ is independent of the trace assignment.

Example 3.1. Let us consider the VENDMACHINE of Fig. 1. Assume that the atomic proposition start holds in state (1), whereas served holds in state (9). Consider the following properties:

$$\begin{split} \varphi_1 &= \forall_{\pi_0}^{\mathsf{base}} \exists_{\pi_1}^{v \wedge s} \exists_{\pi_2}^{v \wedge t} . \Box \big(\mathsf{start}_{\pi_0} \wedge \mathsf{start}_{\pi_1} \wedge \mathsf{start}_{\pi_2} \Longrightarrow \\ & \diamond \mathsf{served}_{\pi_0} \wedge \diamond \mathsf{served}_{\pi_1} \wedge \diamond \mathsf{served}_{\pi_2} \big) \\ \varphi_2 &= \forall_{\pi_0}^{\mathsf{base}} \forall_{\pi_1}^{v \wedge s} \forall_{\pi_2}^{v \wedge t} . \Box \big(\mathsf{start}_{\pi_0} \wedge \mathsf{start}_{\pi_1} \wedge \mathsf{start}_{\pi_2} \Longrightarrow \\ & \diamond \mathsf{served}_{\pi_0} \wedge \diamond \mathsf{served}_{\pi_1} \wedge \diamond \mathsf{served}_{\pi_2} \big) \end{split}$$

The formula φ_1 states that for every trace π_0 from the base variant, there are traces π_1 and π_2 from $[[v \land s]]$ and $[[v \land t]]$ sub-families, such that after the corresponding machines have been *started*, they will eventually *serve* the drink to the customer in all three traces. The formula φ_2 requires the above property to hold for all triples of traces from base, $[[v \land s]]$ and $[[v \land t]]$ sub-families.

4 FAMILY-BASED MODEL CHECKING ALGORITHM

In this section, we present a family-based model checking algorithm for the alternation-free fragment of FMULTILTL, called FMULTILTL₁, in which the series of quantifiers at the beginning of a formula involve zero alternation. For example, the formula φ_2 from Example 3.1 belongs to FMULTILTL₁, but the formula φ_1 does not belong to FMULTILTL₁ since there is one quantifier alternation in it. We assume the FMULTILTL₁ formula to be of the form $\forall^{\psi_1}\pi_1 \ldots \forall^{\psi_n}\pi_n.\phi$. Formulas that are of the form $\exists^{\psi_1}\pi_1 \ldots \exists^{\psi_n}\pi_n.\phi$ can be rewritten as $\forall^{\psi_1}\pi_1 \ldots \forall^{\psi_n}\pi_n.\neg\phi$. Our algorithm extends the standard automata-theoretic approach to model checking [2, 50]. Hence, it uses various automata constructions [50], language non-emptiness, self-composition [3, 49], and a projection operator.

Büchi automata. Büchi automata (BA) [2, 50] are finite-state automata that accept words of infinite length. A BA is a tuple $A = (Q, \Sigma, \delta, Q_0, F)$ where Q is a set of states, Σ is an alphabet, $\delta \subseteq Q \times \Sigma \times Q$ is a transition relation, $Q_0 \subseteq Q$ is a set of initial states, and $F \subseteq Q$ is a set of accepting states. A path $q_0q_1 \ldots \in Q^{\omega}$ of a BA is over a word $w = \alpha_1\alpha_2 \ldots \in \Sigma^{\omega}$, if for all $i \ge 0$, $(q_i, \alpha_{i+1}, q_{i+1}) \in \delta$. A word w is *recognized* by a BA A if there exists a path over the word w with some accepting states from F occurring infinitely often. The *language* $\mathcal{L}(A)$ of a BA A is the set of words that the automaton A recognizes.

Composition. The *n*-fold composition of FTSs $\mathbb{F}_1, \ldots, \mathbb{F}_n$ is the synchronous product $\mathbb{F}_1 \otimes \ldots \otimes \mathbb{F}_n$. Given *n* FTSs defined as $\mathbb{F}_i =$ $(S_i, Act_i, I_i, trans_i, AP, L_i, \mathcal{F}, \mathcal{K}_i, \gamma_i)$ for $1 \le i \le n$, we define the composition $\mathbb{F}_1 \otimes \ldots \otimes \mathbb{F}_n$ as the FTS $(S_1 \times \ldots \times S_n, Act_1 \times \ldots \times Act_n, I_1 \times \ldots \times Act_n, I_1 \times \ldots \times Act_n)$ $\ldots \times I_n$, trans, AP^n , L, \mathcal{F} , $\mathcal{K}_1 \times \ldots \times \mathcal{K}_n$, $\gamma_1 \times \ldots \times \gamma_n$) such that for all states $(s_1, \ldots, s_n), (t_1, \ldots, t_n)$ and actions $(\lambda_1, \ldots, \lambda_n)$, we have $(s_1,\ldots,s_n) \xrightarrow{(\lambda_1,\ldots,\lambda_n)} (t_1,\ldots,t_n) \in trans \text{ iff } s_i \xrightarrow{\lambda_i} t_i \in trans_i \text{ for}$ all $1 \le i \le n$. Moreover, $L : S_1 \times \ldots \times S_n \to 2^{Ap^n}$ such that $Proj_i(L(s_1, ..., s_n)) \subseteq L_i(s_i)$ for all $1 \le i \le n$, where $Proj_i$ is the set obtained by projecting a set of n-tuples to their i-th components. Finally, $\gamma_1 \times \ldots \times \gamma_n ((s_1, \ldots, s_n) \xrightarrow{(\lambda_1, \ldots, \lambda_n)} (t_1, \ldots, t_n)) =$ (ψ_1, \dots, ψ_n) if $\gamma_i(s_i \xrightarrow{\lambda_i} t_i) = \psi_i$ for $1 \le i \le n$. The projection of $\mathbb{F}_1 \otimes \ldots \otimes \mathbb{F}_n$ to a configuration $(k_1, \ldots, k_n) \in \mathcal{K}_1 \times \ldots \times \mathcal{K}_n$, denoted as $Pr_{(k_1,\ldots,k_n)}(\mathbb{F}_1 \otimes \ldots \otimes \mathbb{F}_n)$ is the TS obtained by restricting the transitions of $\mathbb{F}_1 \otimes \ldots \otimes \mathbb{F}_n$ to only those whose feature expressions (ψ_1, \ldots, ψ_n) are satisfied by (k_1, \ldots, k_n) . The semantics $[[\mathbb{F}_1 \otimes \ldots \otimes$ \mathbb{F}_n]]_{*FTS*} is $\cup_{(k_1,\ldots,k_n)\in\mathcal{K}_1\times\ldots\times\mathcal{K}_n}$ [[$Pr_{(k_1,\ldots,k_n)}(\mathbb{F}_1\otimes\ldots\otimes\mathbb{F}_n)$]]_{*TS*}. Let zip denote the function that maps an *n*-tuple of sequences to a single sequence of *n*-tuples. For example, $zip([1, 3, 5, \ldots], [2, 4, 6, \ldots]) =$ $[(1, 2), (3, 4), (5, 6), \ldots]$. Let unzip denote its inverse function. Hence, $\mathbb{F}_1 \otimes \ldots \otimes \mathbb{F}_n$ contains a trace $zip(t_1, \ldots, t_n)$ if $\mathbb{F}_1, \ldots, \mathbb{F}_n$ contain traces t_1, \ldots, t_n , respectively. That is,

 $[\llbracket \mathbb{F}_1 \otimes \ldots \otimes \mathbb{F}_n]]_{FTS} = \{ \mathtt{zip}(t_1, \ldots, t_n) \mid t_i \in [\llbracket \mathbb{F}_i]]_{FTS} \text{ for } 1 \le i \le n \}$ Given an FTS \mathbb{F} , we write $\mathbb{F}^{\psi_1 \otimes \ldots \otimes \psi_n}$ for the composition $Pr_{[\llbracket \psi_1]]}(\mathbb{F}) \otimes \ldots \otimes Pr_{[\llbracket \psi_n]]}(\mathbb{F}).$

Formula-to-automaton construction. Suppose a FMULTILTL₁ formula $\forall^{\psi_1}\pi_1 \ldots \forall^{\psi_n}\pi_n.\phi$ is given. We construct a generalized BA $A_{\phi} = (Q_{\phi}, \Sigma_{\phi}, \delta_{\phi}, Q_{\phi}^0, F_{\phi})$ for ϕ . A generalized BA is the same as a BA except that it has a multiple of accepting states [2]. First, we preprocess ϕ to put it in a negation normal form (NNF) [2]. To construct the states of A_{ϕ} , we define closure(ϕ) to be the set of all sub-formulae of ϕ and their negations. Then we define elementary sets of formulae $B \subseteq \text{closure}(\phi)$ that are maximal

consistent sets with respect to ϕ [2]. When we construct elementary sets of formulae of $closure(\phi)$, we generate *n*-tuples of all atomic propositions that are in that elementary set corresponding to traces π_1, \ldots, π_n . The set of states Q_{ϕ} is the set of elementary sets of formulae of $closure(\phi)$ [2]. Intuitively, a state describes a set of trace tuples where each tuple satisfies all formulae in the elementary set representing that state. The initial set of states is $Q_{\phi}^0 = \{B \in Q_{\phi} \mid \phi \in B\}$. The alphabet is $\Sigma_{\phi} = (2^{AP})^n$, so each letter of the alphabet is an *n*-tuple of sets of atomic propositions. The transition relation $\delta_{\phi} : Q_{\phi} \times \Sigma_{\phi} \times Q_{\phi}$ is given by: if $A = B \cap (AP \cup \{\emptyset\})^n$, then $\delta_{\phi}(B, A)$ is a straightforward extension to *n*-tuples of the standard definition of δ_{ϕ} for LTL [2]. If $A \neq B \cap (AP \cup \{\emptyset\})^n$, then $\delta_{\phi}(B, A) = \emptyset$. The set of accepting states F_{ϕ} contains one set $\{B \in Q_{\phi} \mid \neg(\phi_1 \cup \phi_2) \in B \text{ or } \phi_2 \in B\}$ for each until formula $(\phi_1 \cup \phi_2)$ in closure(ϕ).

The BA A_{ϕ} accepts exactly the words $w \in \mathcal{L}(A_{\phi})$, which are sequences of *n*-tuples, for which $\Pi \models_{\emptyset} \phi$, where $\Pi = [\pi_1 \mapsto proj_1(\text{unzip}(w))] \dots [\pi_n \mapsto proj_n(\text{unzip}(w))]$ (where $proj_i$ denotes the projection of an *n*-tuple to its *i*-th component) and \emptyset is the empty FTS. The construction closely follows the standard LTL automata construction [50], with addition that now we work with *n*-tuple words. In particular, Σ_{ϕ} is $(2^{AP})^n$, so each letter is a *n*-tuple of sets of atomic propositions.

Example 4.1. Consider the formula $\forall f_1 \pi_1 \forall f_2 \pi_2$. $\bigcirc (a_{\pi_1} \land a_{\pi_2})$, where $\phi = \bigcirc (a_{\pi_1} \land a_{\pi_2})$. We have

 $\texttt{closure}(\phi) = \{a_{\pi_1}, a_{\pi_2}, \neg a_{\pi_1}, \neg a_{\pi_2}, a_{\pi_1} \land a_{\pi_2}, \neg (a_{\pi_1} \land a_{\pi_2}), \phi, \neg \phi\}$

The state space Q_{ϕ} consists of the following elementary sets:

 $\begin{array}{ll} B_1 = \{(a_{\pi_1}, a_{\pi_2}), a_{\pi_1} \land a_{\pi_2}, \phi\} & B_2 = \{(a_{\pi_1}, a_{\pi_2}), a_{\pi_1} \land a_{\pi_2}, \neg \phi\} \\ B_3 = \{(a_{\pi_1}, \emptyset), \neg (a_{\pi_1} \land a_{\pi_2}), \phi\} & B_4 = \{(a_{\pi_1}, \emptyset), \neg (a_{\pi_1} \land a_{\pi_2}), \neg \phi\} \\ B_5 = \{(\emptyset, a_{\pi_2}), \neg (a_{\pi_1} \land a_{\pi_2}), \phi\} & B_6 = \{(\emptyset, a_{\pi_1}), \neg (a_{\pi_1} \land a_{\pi_2}), \neg \phi\} \\ B_7 = \{(\emptyset, \emptyset), \neg (a_{\pi_1} \land a_{\pi_2}), \phi\} & B_8 = \{(\emptyset, \emptyset), \neg (a_{\pi_1} \land a_{\pi_2}), \neg \phi\} \end{array}$

The initial states are the states that contain ϕ , $Q_{\phi}^{0} = \{B_{1}, B_{3}, B_{5}, B_{7}\}$. $\delta_{\phi}(B_{1}, \{(a_{\pi_{1}}, a_{\pi_{2}})\}) = \delta_{\phi}(B_{3}, \{(a_{\pi_{1}}, \emptyset)\}) = \delta_{\phi}(B_{5}, \{(\emptyset, a_{\pi_{2}})\}) = \delta_{\phi}(B_{7}, \{(\emptyset, \emptyset)\}) = \{B_{1}, B_{2}\}, \text{ and we have } \delta_{\phi}(B_{2}, \{(a_{\pi_{1}}, a_{\pi_{2}})\}) = \delta_{\phi}(B_{4}, \{(a_{\pi_{1}}, \emptyset)\}) = \delta_{\phi}(B_{6}, \{(\emptyset, a_{\pi_{2}})\}) = \delta_{\phi}(B_{8}, \{(\emptyset, \emptyset)\}) =$

 $\{B_3, B_4, B_5, B_6, B_7, B_8\}$. Note that $\phi = \bigcirc (a_{\pi_1} \land a_{\pi_2}) \in B_1, B_3, B_5, B_7$, so in their next states $(a_{\pi_1} \land a_{\pi_2})$ should hold, and B_1 and B_2 are the only states that contain $(a_{\pi_1} \land a_{\pi_2})$. Similarly, $\neg \phi = \neg \bigcirc (a_{\pi_1} \land a_{\pi_2}) \in B_2, B_4, B_6, B_8$, so in their next states $\neg (a_{\pi_1} \land a_{\pi_2})$ should hold, and B_3, B_4, B_5, B_6, B_7 and B_8 are the states that contain $\neg (a_{\pi_1} \land a_{\pi_2})$. There are no outgoing transitions on other letters. The set F_{ϕ} is empty as ϕ does not contain an until operator, so every infinite run is accepting.

Synchronous product. For an FTS $\mathbb{F}=(S, Act, I, trans, AP, L, \mathcal{F}, \mathcal{K}, \gamma)$ and a BA $A = (Q, 2^{AP}, \delta, Q_0, F)$, the synchronous product is an FTS $\mathbb{F} \otimes A = (S \times Q, Act, trans', I', AP', L', \mathcal{F}, \mathcal{K}, \gamma')$, where AP' = Q and $L'(s, q) = q, (s, q) \xrightarrow{\alpha} '(t, p)$ iff $s \xrightarrow{\alpha} t$ and $q \xrightarrow{L(t)} p, \gamma'((s, q) \xrightarrow{\alpha} '(t, p)) = \gamma(s \xrightarrow{\alpha} t), I' = \{(s_0, q) \mid s_0 \in I, \exists q_0 \in Q_0.(q_0, L(s_0), q) \in \delta\}.$

Model checking results. Our results for family-based model checking of $FMULTILTL_1$ adapt the corresponding results for verification of HyperLTL_1 given in [7].

The algorithm checks $\mathbb{F} \models \forall^{\psi_1} \pi_1 \dots \forall^{\psi_n} \pi_n . \phi$.

- **1** We construct the FTS $\mathbb{F}^{\psi_1 \otimes \ldots \otimes \psi_n}$.
- **2** We construct the Büchi automata A_{ϕ} and $A_{\neg \phi}$.
- **3** We construct the FTS $\mathbb{F}^{\psi_1 \otimes \ldots \otimes \psi_n} \otimes A_{\neg \phi}$.
- 4 We check the persistence property $\mathbb{F}^{\psi_1 \otimes ... \otimes \psi_n} \otimes A_{\neg \phi} \models \Diamond \Box \neg F$, where *F* is the set of accepting states of $A_{\neg \phi}$. If the persistence property does not hold, then the found counterexample corresponds to a counterexample showing that the given FMULTILTL formula is violated by \mathbb{F} . Otherwise, if the persistence property holds, we conclude that the given FMULTILTL formula holds.

Figure 4: The family-based model checking algorithm.

THEOREM 4.2 (FMULTILTL₁). $\mathbb{F} \models \forall^{\psi_1} \pi_1 \dots \forall^{\psi_n} \pi_n \phi$ if and only if (iff) $[[\mathbb{F}^{\psi_1 \otimes \dots \otimes \psi_n} \otimes A_{\neg \phi}]]_{FTS} = \emptyset$

Proof.

$$\begin{array}{l} \forall ^{\psi_1} \pi_1 \ldots \forall ^{\psi_n} \pi_n. \phi \text{ does not hold on } \mathbb{F} \\ \text{iff} \\ \text{there exists a } n \text{-tuple } \Pi_n \in [[\mathbb{F}^{\psi_1 \otimes \ldots \otimes \psi_n}]]_{FTS} \text{ s.t. } \Pi_n \models_{\emptyset} \neg \phi \\ \text{iff} \\ [[\mathbb{F}^{\psi_1 \otimes \ldots \otimes \psi_n} \otimes A_{\neg \phi}]]_{FTS} \text{ is not empty.} \end{array}$$

Algorithm. Our algorithm for verifying FMULTILTL₁ adapts the classical automata-theoretic LTL model checking algorithm [2, 50]. To determine whether an FTS \mathbb{F} satisfies a formula $\forall^{\psi_1} \pi_1 \dots \forall^{\psi_n} \pi_n . \phi$, we call the family-based model checking algorithm illustrated in Fig. 4.

The algorithm in Fig. 4 uses the result from Theorems 4.2 to check FMULTILTL1 formulae. It checks the persistence property $\mathbb{F} \otimes BA \models \Diamond \Box \neg F$, where F is the set of final (accepting) states in the Büchi automaton BA. This reduces to checking if there is a reachable accepting state on a cycle in the FTS $\mathbb{F} \otimes BA$. This is implemented with a double DFS (depth-first search): the outer DFS finds a reachable accepting state, the inner DFS checks whether it is reachable from itself. Both DFS compute the reachability relation of an FTS, and their detailed implementation, denoted CheckPersistence, is given in [12, 13]. The procedure CheckPersistence is based on computing the *reachability relation* of an FTS \mathbb{F} , denoted by $R: S \to \mathcal{P}(\mathcal{K})$, such that for all states $s \in S, k \in R(s)$ iff state s is reachable in the variant $Pr_k(\mathbb{F})$ for configuration k. This procedure generalises the standard DFS algorithm for transition systems, by marking states with sets of configurations, rather than Boolean visited flags. In contrast to the standard DFS for transition systems, where no state is visited twice, this feature-aware DFS can visit states multiple times. When $R(s) = \mathcal{K}'$ and the DFS arrives at state s for the second time with a set of configurations \mathcal{K}'' , such that $\mathcal{K}'' \not\subseteq \mathcal{K}'$, then *s* although already visited, has to be re-explored. This is because some transitions that were disallowed for \mathcal{K}' in s might be allowed for \mathcal{K}'' . We refer to [12, 13] for more details of the procedure CheckPersistence.

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5 IMPLEMENTATION

We have implemented a prototype tool, called DÆDALUX, in C++20 for verifying FMULTILTL₁ formulae. It uses two modelling languages for SPL specification: fPROMELA [10] is a high-level modelling language for describing system families, and TVL [9] is a textual language for describing sets of features \mathcal{F} and valid configurations \mathcal{K} .

fPROMELA is obtained from PROMELA [38] by adding feature variables \mathcal{F} and guarded-by-features statements "gd". PROMELA is a non-deterministic modelling language of the SPIN model checker [38] designed for describing systems composed of concurrent processes that communicate asynchronously. The basic statements of processes are given by:

$$stm ::= skip | x = expr | c?x | c!expr | stm_1; stm_2 |$$

if ::: $g_1 \Rightarrow stm_1 \cdots :: g_n \Rightarrow stm_n :: else \Rightarrow stm fi |$
do :: $g_1 \Rightarrow stm_1 \cdots :: g_n \Rightarrow stm_n$ od

where x is a variable, c is a channel, and g_i are conditions over variables and contents of channels. The "if" is a non-deterministic choice between the statements stm_i for which the guard g_i evaluates to *true* for the current evaluation of the variables. If none of the guards g_1, \ldots, g_n are *true* in the current state, then the "else" statement stm is chosen. Similarly, the "do" represents an iterative execution of the non-deterministic choice among the statements stm_i for which the guard g_i holds in the current state.

TVL [9] is a textual modelling language for describing the set of all valid configurations, \mathcal{K} , for an *f*PROMELA model along with all available features, \mathcal{F} . A feature model is organized as a tree, whose nodes denote features and edges represent parent-child relationship between nodes. The root keyword denotes the root of the tree, and the group keyword, followed by a decomposition type "allof", "someOf", or "oneOf", declares the children of a node. The meaning is that if the parent feature is part of a variant, then "all", "some", or "exactly one" respectively, of its non-optional children have to be part of that variant. The optional features are preceded by the opt keyword. We can also specify different Boolean constraints defined over the features.

The feature variables, \mathcal{F} , used in an *f*PROMELA model are declared as fields of the special type features. The new guarded-by-features statement introduced in *f*PROMELA is of the form:

$$\operatorname{gd} :: \psi_1 \Longrightarrow \operatorname{stm}_1 \ldots :: \psi_n \Longrightarrow \operatorname{stm}_n :: \operatorname{else} \Longrightarrow \operatorname{stm} \operatorname{dg}$$

where ψ_1, \ldots, ψ_n are feature expressions defined over \mathcal{F} . The "gd" is a non-deterministic statement similar to "if", except that only feature variables can be used in conditions (guards). It nondeterministically executes the statement stm_i for which the guard ψ_i evaluate to *true* for the current evaluation of feature variables. If none of guards ψ_1, \ldots, ψ_n is *true*, then the else statement stm is chosen. Hence, "gd" in *f*PROMELA plays the same role as "#ifdef" in C/CPP SPLs [30, 41].

Fig. 5 shows simple *f*PROMELA and TVL models. After declaring feature variables B1 and B2 as well as the global variables n and i in the *f*PROMELA model in Fig. 5 (left), the process foo is defined. The statement 'do :: break :: n++ od' is used to non-deterministically initialize variables n and i of type byte to any integer value from their domain [0, 255] at label Start. The first gd statement specifies that i=i+2 is available for variants that contain the feature B1, and skip

for variants with ¬B1. The second gd statement is similar, except that the guard is the feature B2. It states that i=i+1 is available for variants containing B1 and skip for variants with ¬B1. Finally, we print out the current value of i at label Final. The TVL model in Fig. 5 (right) specifies four valid configurations: {Main, B1, {Main, B1}, {Main, B2}, {Main, B1, B2} for this system family. Finally, we specify FMULTILTL properties:

$$\begin{array}{l} \varphi_1 = \forall_{\pi_1}^{\mathsf{B}1} \forall_{\pi_2}^{\mathsf{B}2} \cdot (\mathsf{Start} \land \mathsf{n}_{\pi_1} = \mathsf{n}_{\pi_2}) \implies \diamondsuit (\mathsf{Final} \land i_{\pi_1} \ge i_{\pi_2}) \\ \varphi_2 = \exists_{\pi_1}^{\mathsf{B}1} \exists_{\pi_2}^{\mathsf{B}2} \cdot (\mathsf{Start} \land \mathsf{n}_{\pi_1} = \mathsf{n}_{\pi_2}) \implies \diamondsuit (\mathsf{Final} \land i_{\pi_1} \ge i_{\pi_2}) \end{array}$$

The property φ_1 states that for all traces π_1 from the sub-family [[B1]] and π_2 from [[B2]], if the value of n in the label Start is the same in traces π_1 and π_2 , then eventually $i_{\pi_1} \ge i_{\pi_2}$ will hold in label Final. The property φ_1 does not hold. The counter-example for φ_1 contains a trace $\pi_1 \in Pr_{B1\land \neg B2}(\mathbb{F}) \subseteq Pr_{[[B1]]}(\mathbb{F})$ (where \mathbb{F} is the FTS for *f* PROMELA model in Fig. 5), in which i=n+2 in label Final (where n is the initial value of variable n), and a trace $\pi_2 \in Pr_{B1\land B2}(\mathbb{F}) \subseteq Pr_{[[B2]]}(\mathbb{F})$, in which i=n+3 in label Final.

The property φ_2 states that there exist traces π_1 from [[B1]] and π_2 from [[B2]], if the value of n in Start is the same in π_1 and π_2 , then eventually $i_{\pi_1} \ge i_{\pi_2}$ in Final. The property φ_2 holds, and the witness is a trace $\pi_1 \in Pr_{B1/B2}(\mathbb{F}) \subseteq Pr_{[[B1]]}(\mathbb{F})$ in which i=n+3 in Final and a trace $\pi_2 \in Pr_{\neg B1/B2}(\mathbb{F}) \subseteq Pr_{[[B2]]}(\mathbb{F})$ in which i=n+1 in Final. We verify φ_2 by encoding it as $\varphi'_2 = \forall_{\pi_1}^{B1} \forall_{\pi_2}^{B2} \cdot \neg((\text{Start} \land n_{\pi_1} = n_{\pi_2}) \implies \diamondsuit(\text{Final} \land i_{\pi_1} \ge i_{\pi_2}))$, which is equivalent to $\forall_{\pi_1}^{B1} \forall_{\pi_2}^{B2} \cdot (\text{Start} \land n_{\pi_1} = n_{\pi_2}) \land \Box(\neg \text{Final} \lor i_{\pi_1} < i_{\pi_2})$. A negative answer to φ'_2 represents a positive answer to φ_2 , and vice versa. That is, the counter-example violating φ'_2 represents a witness showing that φ_2 is correct.

We now give a brief overview of the *f* PROMELA semantics [10]. Similarly as a PROMELA model defines a program graph (PG) [2], an *f*PROMELA model defines a so-called featured program graph (FPG) [10] that formalizes the control flow of the model. The vertices of the graph are control locations and transitions are annotated with *condition/effect/feature expression* triples. The "gd" statement specifies the feature expression part of transitions. The *semantics* of an FPG is an *FTS* obtained from "*unfolding*" the graph (see [2, Sect. 2] for details). The FPG of our *f*PROMELA model in Fig. 5 is shown in Fig. 6. The unfolded FTS can be easily constructed, such that each state in it contains the information about the control location (line number) and the current value of variables n and i.

The family-based model checking algorithm is executed *on-the-fly*, by constructing the product FTS $\mathbb{F} \otimes BA$ "on-demand", where \mathbb{F} is the FTS of the system family and *BA* is the Büchi automaton of the negated formula we consider. The generation of reachable states of \mathbb{F} proceeds in parallel with the construction of the relevant fragment of *BA*. When generating the successors of a state in *BA*, we only need to consider the successors matching the current state of \mathbb{F} . Hence, we can find an accepting state of *BA* on a cycle, without the need to generate the entire *BA*.

6 EVALUATION

We now evaluate our approach for family-based model checking of $FMULTILTL_1$ properties using a new proof-of-concept tool, which we integrated within a new SPL model checking platform called

0 typedef features { 1 bool B1; bool B2; } 2 features f; 3 byte n, i; 4 active proctype foo() { 0 root Main { 5 do :: break :: n++ od; group allOf { 6 Start: i := n: opt B1, 2 $gd :: f.B1 \Rightarrow i=i+2 :: else \Rightarrow skip dg;$ 7 3 opt B2 $gd :: f.B2 \Rightarrow i=i+1 :: else \Rightarrow skip dg;$ 8 } } 4 Final: printf("i : %d", i); 9 10 }

```
11 A{p1}[B1] A{p2}[B2]((foo@Start && n{p1}==n{p2}) \rightarrow 11 \qquad \diamondsuit(foo@Final && i{p1} \ge i{p2}))
```

Figure 5: Simple *f* PROMELA (left) and TVL (right) models



Figure 6: An FPG. The state "lx" refers to the line number x in the model foo in Fig. 5, and tt is short for true.

DAEDALUX.¹ The evaluation aims to show that we can verify some interesting properties over model families that are not expressible in the existing logic. Moreover, we want to test and determine the performance limits of the current implementation, and so set the scene for improvements and extensions of our approach in future.

6.1 Experimental setup

Experiments are executed on a DELL latitude 7310, 64-bit Intel[®]CoreTM vPro 10th gen CPU@2.3GHz, Ubuntu 20.10, with 16 GB memory, and we use a timeout value of 60 seconds. All times are reported as average over five independent executions.

For each experiment, we report: TIME which is the time to model check in seconds (this includes the times to parse the fPROMELA model, to build the initial FTS, and to run the model checking algorithm); and SPACE which is the memory occupied in MB to perform the given model checking task.

The evaluation is performed on two benchmarks: Synthetic and MinePump model families [10, 11], by verifying various FMULTILTL1 properties.

6.2 Synthetic example

Combinatorically, the number of variants in \mathcal{K} grows exponentially with the number of features $|\mathcal{F}|$, which means that there is an exponential blow-up in the model checking strategy for LTL that verifies all variants one by one. Although, DAEDALUX implements specialized family-based model checking algorithms of LTL that check all variants simultaneously in a single run, its performance still depends on the size and complexity of the configuration space \mathcal{K} . Unfortunately, model checking of FMULTILTL is even harder than LTL because, another source of complexity is stemming from the *n*-fold composition operator and the need to work with *n*-sized tuples. The size of the synchronous product (*n*-fold composition) increases exponentially with the number of copies. Thus, reasoning on the product model becomes computationally very prohibitive even for smaller values of *n*.

As an experiment, we have tested the limits of our family-based model checking algorithm for FMULTILTL₁. We have gradually added variability to the model family in Fig. 5, and we have also generated bigger FMULTILTL₁ formulae with bigger number of quantifiers. We write |Q| to denote the number of quantifiers in a FMULTILTL₁ formula. This was done by adding unconstrained optional features and by sequentially composing gd statements guarded by all existing features. Note that we have $\mathcal{K} = 2^{|\mathcal{F}|}$, since all features are optional. For example, the *f*PROMELA process *foo* with three features B1, B2, and B3 is:

do :: break :: n++ od; Start: i := n; gd :: $f.B1 \Rightarrow i=i+3$:: else \Rightarrow skip dg; gd :: $f.B2 \Rightarrow i=i+2$:: else \Rightarrow skip dg; gd :: $f.B3 \Rightarrow i=i+1$:: else \Rightarrow skip dg; Final: printf("i: %d", i);

and the corresponding properties with three quantifiers are:

$$\begin{split} \varphi_1 &= \forall_{\pi_1}^{\mathsf{B}} \forall_{\pi_2}^{\mathsf{B}2} \forall_{\pi_3}^{\mathsf{B}3}. (\mathsf{Start} \land \mathsf{n}_{\pi_1} = \mathsf{n}_{\pi_2} = \mathsf{n}_{\pi_3}) \Longrightarrow \\ &\qquad \diamond (\mathsf{Final} \land i_{\pi_1} \ge i_{\pi_2} \land i_{\pi_2} \ge i_{\pi_3}) \\ \varphi_2 &= \exists_{\pi_1}^{\mathsf{B}1} \exists_{\pi_2}^{\mathsf{B}2} \exists_{\pi_3}^{\mathsf{B}3}. (\mathsf{Start} \land \mathsf{n}_{\pi_1} = \mathsf{n}_{\pi_2} = \mathsf{n}_{\pi_3}) \Longrightarrow \\ &\qquad \diamond (\mathsf{Final} \land i_{\pi_1} \ge i_{\pi_2} \land i_{\pi_2} \ge i_{\pi_3}) \end{split}$$

Table 1 compares the effect in terms of both TIME and SPACE of analyzing the synthetic example for different sizes of $|\mathcal{F}|$ and

¹https://github.com/samilazregsuidi/Daedalux

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	Q = 2		Q = 4		Q = 6		$ Q = \mathcal{F} $	
$ \mathcal{F} $	Тіме	Space	Тіме	Space	Тіме	Space	Time	Space
6	0.097	15.0	0.112	17.7	0.163	28.9	0.163	28.9
7	0.098	15.1	0.114	18.5	0.188	33.2	0.435	69.6
8	0.097	15.2	0.127	19.6	0.219	37.9	0.869	139.8
9	0.100	15.3	0.125	20.2	0.250	42.8	1.708	308.6
10	0.103	15.5	0.129	21.2	0.261	48.2	3.637	716.4
11	0.104	15.7	0.142	21.5	0.292	53.8	8.755	1699.2
14	0.124	16.1	0.153	23.5	0.302	59.8	15.89	2664.2
40	0.185	17.6	0.190	34.1	0.344	123.8	$-\star$ infeasible \star -	

Table 1: Verification of the property φ_1 of the Synthetic example. Time in seconds and Space in MB.

|Q|. We report only the performance results for the property φ_1 , since we obtain similar results for φ_2 . We observe that the occupied memory SPACE grows exponentially with the number of features $|\mathcal{F}|$ and quantifiers |Q| (when $|Q| = |\mathcal{F}|$), thus representing the bottleneck of the verification task. In fact, the size of the explored model spaces increases very rapidly with the size of the tuples, making the reasoning on the models very prohibitive. Note that the size of tuples is identical to the number of quantifiers |Q| in the given property. Figure 7 (left) depicts this phenomenon. It shows the occupied memory (in MB) of using DAEDALUX to verify property φ_1 for increasing number of features and quantifiers, when $|Q| = |\mathcal{F}|$. Figure 7 (right) shows the accumulated time (in sec) for increasing number of features and quantifiers, when $|Q| = |\mathcal{F}|$. We can see that the time also grows exponentially with $|\mathcal{F}|$ and |Q|. Already for $|Q| = |\mathcal{F}| = 14$, the occupied memory to check the property becomes 2,664 MB and the analysis time becomes 15.89 sec. The tool crashes for bigger values of $|Q| = |\mathcal{F}|$ due to the enormous memory consumption (>10GB).

On the other hand, if the number of quantifiers |Q| is fixed (|Q| = 2, 4, or 6), we observe only linear growth of TIME and SPACE for increasing number of features $|\mathcal{F}|$. This is due to the fact that we work with the same sized tuples in those cases and the DAEDALUX tool can efficiently handle the variability in this SYNTHETIC model family. For example, we can successfully verify the property even for $|\mathcal{F}| = 40$ (see Table 1).

6.3 MINEPUMP example

The MINEPUMP system was introduced in the CONIC project [42]. Based on the original system, an *f*PROMELA model was created in [11] as part of the SNIP project. The *f*PROMELA MINEPUMP family contains about 200 LOC and 7 (non-mandatory) independent optional features: Start, Stop, MethaneAlarm, MethaneQuery, Low, Normal, and High, thus yielding $2^7 = 128$ variants. Its FTS has 21,177 states and all variants combined have 889,252 states. It consists of 5 communicating processes: a controller, a pump, a watersensor, a methanesensor, and a user. When activated, the controller should switch on the pump when the water level is high, but only if there is no methane in the mine.

By setting the variable pstate the controller can be found in one of the following states: running, ready, stopped, methanstop, lowstop. We consider the following FMULTILTL₁ property that

checks the correlation between the variable pstate that the controller uses to manage the pump actuator and the property that the pump is switched on or off (via the Boolean variable pumpOn):

$$\varphi = \forall_{\pi_1}^{\text{MethaneAlarm}} \forall_{\pi_2}^{\text{MethaneQuery}} . (\text{pstate}_{\pi_1} = \text{pstate}_{\pi_2}) \implies \\ \diamond (\text{pumpOn}_{\pi_1} = \text{pumpOn}_{\pi_2})$$

That is, for all traces π_1 from [[MethaneAlarm]] sub-family and all traces π_2 from [[MethaneQuery]] sub-family, if at some point the controller states are equal, then eventually the pump activities that follow should be the same. We have found that the property φ does not hold, and the reported violation is witnessed by two infinite traces from the variant: Start \land Stop \land MethaneAlarm \land MethaneQuery \land Low \land High. This variant is present in both subfamilies [[MethaneAlarm]] and [[MethaneQuery]]. To verify φ , the DAEDALUX tool takes 65.7 seconds and 2.95 GB memory. Similarly, we can verify the satisfaction of the dual FMULTILTL₁ property:

$$\varphi = \exists_{\pi_1}^{\text{MethaneAlarm}} \exists_{\pi_2}^{\text{MethaneQuery}} . (pstate_{\pi_1} = pstate_{\pi_2}) \implies \\ \diamondsuit (pumpOn_{\pi_1} = pumpOn_{\pi_2})$$

6.4 Discussion

Our proof-of-concept model checker for the alternation-free fragment of FMULTILTL is limited to smaller system families and smaller properties as evidenced by experiments. It represents a demonstration that model checking of FMULTILTL properties is possible. However, the verification task becomes computationally very demanding for more realistic systems like the MINEPUMP. In the future work, we aim to propose some optimization heuristics that will reduce the computational complexity of model checking FMULTILTL₁ in practice, and thus enable us to handle bigger realworld case studies and bigger properties as well as other more complex fragments of FMULTILTL. We also envision to leverage modern verification techniques like IC3 [46], interpolation [43], SMT [18] to improve the current algorithms on model checking of FMULTILTL.

7 RELATED WORK

In the last two decades, researchers have introduced various familybased (lifted) analysis and verification techniques for SPLs. Some successful examples range from family-based syntax and type checking [36, 40, 41], to family-based static analysis [4, 23, 27–29, 31, 51]. Family-based model checking has also been an active research field,



Figure 7: The performance of family-based model checking with DAEDALUX as a function of the number of features $|\mathcal{F}|$ and quantifiers |Q| (when $|Q| = |\mathcal{F}|$). The x-axis represents the number of features and quantifiers, and the y-axis represents the occupied memory in MB (left) and verification time in seconds (right).

where different approaches have been developed for verifying system and program families. Among various modelling formalisms for representing SPLs, we focus here on FTSs. We divide our discussion of related work into three categories: family-based model checking on FTSs, family-based software model checking, and temporal logics for hyper- and multi-properties.

Family-based model checking on FTSs. Featured transition systems (FTSs) are today widely accepted formalism for representing system families (SPLs). Specialized family-based model checking algorithms have been designed for verifying FTSs against LTL properties [11]. They have been implemented in the SNIP family-based model checker [10] and its successor PROVELINES [15]. Cordy et. al [17] have also introduced symbolic family-based model checking algorithms for verifying FTSs against CTL properties, which has been implemented as an extension of the NuSMV model checker. Familybased model checking has been also defined for verifying μ -calculus properties using the general-purpose mCRL2 model checker [47], whereas family-based model checking for verifying probabilistic system families has been defined in [6] and implemented in the PRO-FEAT tool. To make all these algorithms based on FTSs more scalable, various abstractions have been applied. The so-called variability abstractions and the automatic abstraction-refinement procedures for efficient family-based model checking of LTL are proposed in [26, 34]. Subsequently, the above procedures have been extended for verifying CTL and μ -calculus properties [20, 32]. Abstractionrefinement procedures for family-based model checking have also been proposed for LTL and CTL properties of reactive system families [16, 32] and reachability properties of probabilistic system families [5]. They have been applied to synthesis for resolving program and model sketches [24, 25]. In this paper, we pursue this line of work by proposing specifically designed family-based model checking algorithms for verifying FMULTILTL properties of FTSs.

Family-based software model checking. Family-based model checking algorithms have also been used for verifying program families. The variability encoding approach [1, 39, 52] generates a family *simulator*, which represents a single program simulating the behaviour of all variants in the given program family. Then a standard off-the-shelf software model checker is used to verify the generated family simulator, so that an incorrect variant can be identified from a found counterexample. However, this algorithm stops once

a single counterexample is found, so apart from the variant corresponding to the found counterexample the other variants cannot be classified as correct or incorrect. This approach was used for model checking C program families implemented using compositional approaches [1, 52] and using #ifdef annotations from the CPP preprocess [39].

A game semnatics approach for family-based software model checking has been introduced in [19, 21]. Special family-based model checking algorithms are designed over symbolic game semantics models that are compact representations of #ifdef-based programs containing undefined components (free identifiers). This way, the approach can verify safety properties of program families.

Temporal logics for hyper- and multi-properties. Hyper-properties [8] represent a formalism for specifying properties of sets of traces, by quantification over traces in the system. They are especially suitable for specifying security properties, such as secure information flow and non-interference. The logic HyperLTL and HyperCTL* have been introduced in [7]. This work also proposes one of the first algorithms for model checking hyper-properties by combining self-composition and the classical LTL model checking. Selfcomposition combines several disjoint copies of the same system, allowing to express relationships among multiple traces. Subsequently, more scalable approach has been defined using alternating Büchi automaton [35]. The notion of hyper-properties is generalized to multi-properties in [37], which describes the behaviour of not just a single system, but of a set of systems called multimodel. While hyper-properties relate traces from the same system, multi-properties relate traces from the different components in the multi-model. Goudsmid et. al [37] introduce direct algorithms for model checking multi-properties from the MULTILTL logic. In this work, we further generalize the notion of multi-properties to FMULTILTL logic, which explicitly relates traces from the various sub-families of a system family (SPL).

8 CONCLUSION

In this work, we proposed a new FMULTILTL logic for specifying multi-properties of system families. We have described an algorithm for model checking of FMULTILTL₁ fragment of the new logic. An implementation in the DAEDALUX tool is applicable to quantifier-free FMULTILTL properties. The evaluation confirms that some interesting properties can be efficiently verified in this way.

However, it also establishes that reasoning on the self-composed products is computationally very demanding.

In the future, we want to develop family-based algorithms for model checking other more complex fragments of FMULTILTL, such as the FMULTILTL₂ fragment that contains formulas in which the series of quantifiers at the beginning of a formula may involve at most one alternation. That is, FMULTILTL₂ formulas are of the form $\forall \psi_1 \pi_1 \dots \forall \psi_l \pi_l \exists \psi_{l+1} \pi_{l+1} \dots \exists \psi_{l+j} \pi_{l+j} .\phi$. We also plan to employ abstraction-based techniques [26, 34] to avoid the construction of the full product. We can use abstractions to compute approximations of all sub-families represented in the full product, such that if model checking the abstract full product is successful, we conclude that model checking the original full product holds. Since the abstract sub-families are much smaller models than the original ones, we can use this technique for accelerating model checking of multi-properties.

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